

This specific equation is called the Born Interpretation (or Born's Rule) of the wavefunction. It was formulated by physicist Max Born in 1926, a discovery that earned him the Nobel Prize.

In short, this equation is the bridge between abstract quantum mathematics and real-world reality. It tells us how to translate a mathematical wavefunction ( $\Psi$ ) into something we can actually measure in a lab: probability.

Here is the exact mathematical breakdown of what each part of this equation is doing.

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## 1. $P(\mathbf{r}, t)$ — The Probability Density

The left side of the equation represents Probability Density at a specific position ( $\mathbf{r}$ ) and a specific time ( $t$ ).

Crucial Distinction: It is a probability density, not a flat probability.

Because space is continuous, the probability of a particle being at an infinitesimally exact point is zero. Instead,  $P(\mathbf{r}, t)$  tells you the probability per unit volume.

To find the actual probability of finding a particle in a small region of space (like a tiny box of volume  $dV$ ), you multiply the density by that volume:  $P \cdot dV$ .

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## 2. $|\Psi(\mathbf{r}, t)|^2$ — The Absolute Square

The wavefunction  $\Psi(\mathbf{r}, t)$  itself is a complex number (it contains the imaginary unit  $i = \sqrt{-1}$ ).

Because instruments in a lab can only measure real physical quantities (like meters, seconds, or Joules), a complex number cannot directly represent a physical measurement. You can't have a meter stick measure an "imaginary" distance.

By taking the absolute square ( $|\Psi|^2$ ), the mathematics strips away the imaginary components and forces the result to be a positive, real number. This maps perfectly onto the concept of probability, which must always be a real number between 0 and 1.

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## 3. $\Psi^*(\mathbf{r}, t)\Psi(\mathbf{r}, t)$ — How It's Calculated

This third part shows you the actual algebraic step used to find the absolute square of a complex function.

In complex algebra, to find the square of the magnitude of a complex number, you multiply that number by its complex conjugate (denoted by the asterisk ).

> How it works mathematically: > If a wavefunction at a certain point evaluates to the complex number  $z = a + bi$ , its complex conjugate is  $z^* = a - bi$  (you just flip the sign of the imaginary part). > When you multiply them together: > >

$$|\Psi|^2 = \Psi^* \Psi = (a - bi)(a + bi) = a^2 + abi - abi - b^2 i^2$$

> > > > Since  $i^2 = -1$ , this simplifies to: > >

$$|\Psi|^2 = a^2 + b^2$$

> >

The imaginary parts completely cancel out, leaving you with a pure, positive real number.

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## Conceptual Summary

Before you measure a quantum particle (like an electron), it does not exist in one definitive place. It exists in a "superposition of states"—a cloud of possibilities described by  $\Psi$ .

When you evaluate  $\Psi^*(r, t)\Psi(r, t)$ :

Areas where the result is high mean you have a very high chance of detecting the particle there when you look.

Areas where the result is zero mean you will absolutely never find the particle there.

This equation turned quantum mechanics from a theory about literal "matter waves" into a theory about waves of probability.

# Document information

## Born Interpretation

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<b>Project</b>	Scrodinger Equation
<b>Document</b>	Document 1.1.1
<b>Author</b>	mujirin
<b>Verifier</b>	Not verified
<b>Downloaded</b>	July 03, 2026 21:26 KST
<b>Status</b>	Working
<b>Document link</b>	<a href="https://theorytrace.com/projects/scrodinger-equation/documents/pmathbfr-t-psimathbfr-t2-psimathbfr-tpsimatehbf-t/">https://theorytrace.com/projects/scrodinger-equation/documents/pmathbfr-t-psimathbfr-t2-psimathbfr-tpsimatehbf-t/</a>